Extra Practice

Chapter 6

Lesson 6-1

Simplify each radical expression. Use absolute value symbols as needed.

1.
$$\sqrt{36x^4}$$

2.
$$\sqrt{c^{80}d^{50}}$$

3.
$$\sqrt[4]{81x^{12}}$$

5.
$$\sqrt[5]{-32k^5}$$

6.
$$\sqrt[4]{\frac{1}{16}w^{12}}$$

7.
$$\sqrt[4]{m^{18}n^8}$$

8.
$$\sqrt[3]{27y^{15}}$$

9.
$$\sqrt[5]{-243r^{20}}$$

- **10.** You can use the expression $D = 1.2 \sqrt{h}$ to approximate the visibility range D, in miles, from a height of h feet above ground.
 - **a.** Estimate the visibility from a height of 900 feet.
 - **b.** How far above ground is an observer whose visibility range is 84 miles?
- 11. You can approximate the speed of a falling object as $v = 8\sqrt{d}$, where v is the speed in feet per second and d is the distance, in feet, the object has fallen. Express d in terms of v.

Lesson 6-2

Multiply or divide and simplify. Assume that all variables are positive.

12.
$$\sqrt{3x^4}$$
. $\sqrt{24x^3}$

13.
$$\sqrt[3]{4}.\sqrt[3]{18}$$

14.
$$\sqrt{5a^3}$$
 $\sqrt{20a}$

15.
$$\frac{\sqrt{80}}{\sqrt{5}}$$

16.
$$\frac{\sqrt{18x^5y}}{\sqrt{2x}}$$

$$17. \ \frac{\sqrt[3]{640w^3z^8}}{\sqrt[3]{5wz^4}}$$

18. The time *T* it takes a pendulum to make a full swing in each direction and return to its original position is called the period of the pendulum. The equation $T = 2\pi \sqrt{\frac{1}{32}}$ relates the length of the pendulum , in feet, to its period T, in seconds. How long is a pendulum if its period is 3 seconds? Round the answer to the nearest tenth.

Lesson 6-3

Simplify.

19.
$$2\sqrt{7} + 3\sqrt{7}$$

20.
$$\sqrt{32} + \sqrt{8}$$

21.
$$\sqrt{7x} + \sqrt{28x}$$

22.
$$3\sqrt{18} + 2\sqrt{72}$$

23.
$$\sqrt{27} + \sqrt{48}$$

24.
$$8\sqrt{45} - 3\sqrt{80}$$

25.
$$(2+\sqrt{5})(3+\sqrt{5})$$

26.
$$(6-\sqrt{7})(1-\sqrt{7})$$

27.
$$(\sqrt{10} + 3)^2$$

25.
$$(2+\sqrt{5})(3+\sqrt{5})$$
 26. $(6-\sqrt{7})(1-\sqrt{7})$ **28.** $(3\sqrt{5}-2)(3\sqrt{5}+2)$ **29.** $\frac{5}{2-\sqrt{3}}$

29.
$$\frac{5}{2-\sqrt{3}}$$

30.
$$\frac{4-3\sqrt{7}}{1+2\sqrt{7}}$$

Extra Practice (continued)

Chapter 6

Lesson 6-4

Write each expression in simplest form. Assume that all variables are positive.

31.
$$81^{\frac{1}{2}}$$

32.
$$36^{\frac{1}{4}} \cdot 36^{\frac{1}{4}}$$

33.
$$\left(x^{-\frac{4}{3}}y^{\frac{3}{5}}\right)^{15}$$

34.
$$\left(x^{\frac{1}{4}}y^{-\frac{3}{8}}\right)^{16}$$

35.
$$(8x^{15}y - 9)^{-\frac{1}{3}}$$

36.
$$\left(-27x^{-9}y^6\right)^{\frac{1}{3}}$$

37.
$$\left(-32x^{-10}y^{15}\right)^{\frac{1}{5}}$$

38.
$$(32x^{20}y^{-10})^{-\frac{1}{5}}$$

39.
$$\left(\frac{81y^{16}}{16x^{12}}\right)^{\frac{1}{4}}$$

40.
$$\left(\frac{16x^{14}}{81y^{18}}\right)^{\frac{1}{2}}$$

41.
$$\sqrt{5} \cdot \sqrt[3]{5}$$

42.
$$\frac{\sqrt[6]{x^2}}{\sqrt[3]{x^5}}$$

Lesson 6-5

Solve. Check for extraneous solutions.

43.
$$\sqrt{13x-10} = 3x$$

44.
$$\sqrt{x+20} = x$$

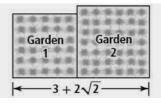
45.
$$(4x-12)^{\frac{1}{2}}+3=x$$

46.
$$(7x)^{\frac{1}{3}} = (5x+2)^{\frac{1}{3}}$$

47.
$$\sqrt{x-2} - \sqrt{2x+3} = -2$$

48.
$$\sqrt{10x} - 2\sqrt{5x - 25} = 0$$

- **49.** A community garden offers two different square-shaped plots of growing space as shown. The larger plot measures one square meter greater than the smaller one. The combined lengths of the two gardens is $3 + 2\sqrt{2}$ meters.
 - a. What is the area of Garden 1?
 - **b.** What is the length of Garden 2?



Lesson 6-6

Let $f(x) = 3x^2$ and g(x) = 2 - 5x. Perform each function operation.

50.
$$f(x) - g(x)$$

51.
$$f(x) \cdot g(x)$$

$$52. \ \frac{f(x)}{g(x)}$$

53.
$$(f+g)(x)$$

54.
$$(f \cdot g)(x)$$

55.
$$\frac{g}{f}(x)$$

Let $f(x) = x^2$ and g(x) = 3x + 1. Evaluate each expression.

56.
$$(f \circ g)(0)$$

57.
$$(f \circ g)(2)$$

58.
$$(f \circ g)(23)$$

59.
$$(f \circ g)(5)$$

60.
$$(g \circ f)(0)$$

61.
$$(g \circ f)(1)$$

62.
$$(g \circ f)(-1)$$

63.
$$(f \circ f)(3)$$

64.
$$(g \circ g)(4)$$

Extra Practice (continued)

Chapter 6

- 65. Halina works in a department store. Three times per year she is allowed to combine her employee discount with special sale prices. Let x be the retail price of a blouse.
 - **a.** Halina's employee discount is 20%. Write a function E(x) that represents the cost of the blouse after the discount.
 - **b.** Due to a manufacturer's incentive, the blouse is marked down 25%. Write a function M(x) that represents the sale price.
 - **c.** The sales tax on clothing is 6%. Write a function T(x) that describes the cost of a clothing item with sales tax included.
 - **d.** Halina found a blouse to which the discounts apply. Use the function composition $f = T \circ E \circ M$ to write the function f(x) that represents the price Halina will pay for the blouse.
- **66.** You invest p dollars in an account that earns a simple interest of 6%. The function that represents the account balance at the end of the year is f(p) = 1.06p.
 - a. Suppose that at the end of the year you deposit \$500 in the account. Write a new function g(p) that shows the balance that will earn interest in the second year.
 - **b.** At the end of every year you add \$500 to the account. The interest rate remains 6%. Write a composition of functions f and g to find the account balance at the end of the third year, before adding the \$500. Find that balance for an initial investment of \$1000.

Lesson 6-7

For each function f, find f^{-1} and the domain and range of f and f^{-1} . Determine whether f^{-1} is a function.

67.
$$f(x) = 6x + 1$$

68.
$$f(x) = \sqrt{x+4}$$

67.
$$f(x) = 6x + 1$$
 68. $f(x) = \sqrt{x+4}$ **69.** $f(x) = \sqrt{x-3}$

70.
$$f(x) = \sqrt{-5x + 2}$$
 71. $f(x) = 3x^2 + 1$ **72.** $f(x) = 2 - x^2$

71.
$$f(x) = 3x^2 + 1$$

72.
$$f(x) = 2 - x^2$$

Extra Practice (continued)

Chapter 6

- **73.** You can use the function f(x) = 331.4 + 0.6x to approximate the speed of sound in dry air, where *x* is the temperature in degrees Celsius.
 - **a.** Write an algebraic expression for the inverse function $f^{-1}(x)$.
 - **b.** Evaluate $f^{-1}(x)$ for x 5 350. Round the result to the nearest whole number. Explain what your result represents.

Lesson 6-8

Graph each function.

74.
$$y = \sqrt{x}$$

75.
$$y = \sqrt{x} - 1$$

76.
$$y = \sqrt{x} + 3$$

77.
$$y = \sqrt{x+3}$$

78.
$$y = 4\sqrt{x}$$

79.
$$y = \frac{3}{4}\sqrt{x}$$

80.
$$y = 2\sqrt{x-5} + 2$$

81.
$$y = \sqrt[3]{x+1}$$

82.
$$y = \sqrt[3]{x-2} - 3$$